

Appln. Serial No. 09/990,542  
Amendment Dated August 30, 2005  
Reply to Office Action Mailed June 30, 2005

### AMENDMENTS TO THE CLAIMS

This listing of claims replaces all prior versions, and listings, of claims in the application:

- 1 1. (Previously Presented) A method for producing, for a target computer architecture and a  
2 program fragment, a near-optimal code sequence for executing the program fragment on the  
3 target computer, comprising:  
4 repeatedly invoking an automatic theorem prover for plural cycle budgets to  
5 determine a minimum cycle budget that is the lowest of any cycle budget K for  
6 which a formalized mathematical conjecture that no code sequence for the target computer  
7 architecture executes the program fragment within the cycle budget K is unprovable by the  
8 automatic theorem prover, and  
9 extract the near optimal code sequence from a counterexample implicit in the  
10 failed proof of the formalized mathematical conjecture for the minimum cycle budget.
- 1 2. (Previously Presented) The method of claim 1, wherein the automatic theorem prover is  
2 two-phased, the two phases including  
3 instantiating facts by a matcher about machine operations that are computable by a  
4 machine with the target computer architecture and facts about non-machine operations, followed  
5 by  
6 a boolean satisfiability search.
- 1 3. (Original) The method of claim 1, wherein the program fragment specifies a vector of  
2 expressions to be computed together with one or more of  
3 a vector of target destinations into which the values of the expressions are to be placed,  
4 and  
5 a guard and label pair, the guard being a given boolean expression that determines  
6 whether the program fragment is to be executed as described or whether, instead, control is to be  
7 transferred to the label.

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- 1 4. (Original) The method of claim 1, wherein, during the invocations of the automatic  
2 theorem prover, the minimum number of machine cycles for each successive invocation is set to  
3 a value so as to bisect the interval of remaining possible values of the minimum number of  
4 machine cycles.
- 1 5. (Original) The method of claim 2, wherein the instantiated facts from the matcher are  
2 asserted into an e-graph which is formed from a term graph augmented by an equivalent relation  
3 connecting terms known to be equal.
- 1 6. (Original) The method of claim 2, wherein the satisfiability search operates on a  
2 collection of boolean unknowns that encode a set of conjectured code sequences for a machine  
3 with the target computer architecture, each of these code sequences being defined in terms of a  
4 set of machine operations initiated in each cycle.
- 1 7. (Original) The method of claim 6, wherein the instantiated facts from the matcher are  
2 asserted into an e-graph which is formed from a term graph augmented by an equivalent relation  
3 connecting terms known to be equal, and wherein the encoding is performed such that, for each  
4 term of the e-graph and each cycle *i* of the minimum number of machine cycles for a particular  
5 invocation, there is a particular boolean unknown that indicates whether the conjectured code  
6 sequence performs a computation of the root operation of the term during cycle *i*.
- 1 8. (Previously Presented) The method of claim 6, wherein the boolean unknowns encode  
2 boolean constraints suitable for the target computer architecture.

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1 9. (Previously Presented) A method for producing, for a target computer architecture and a  
2 program fragment, a near-optimal code sequence for executing the program fragment on the  
3 target computer, comprising:

4 repeatedly invoking an automatic theorem prover to prove unsatisfiable a formalized  
5 mathematical conjecture that, for a cycle budget K, no code sequence for the target computer  
6 architecture executes the program fragment within that cycle budget K,

7 wherein if the proof fails, a K-cycled program computing the program fragment is  
8 embedded in the failed proof,

9 wherein the near-optimal code sequence is found, and the invocation need not be  
10 repeated, when it is established that both the K-cycled program computes the program fragment  
11 and a cycle budget K-1 is insufficient in that the cycle budget K is minimum, the K-cycled  
12 program being extracted as the near-optimal code sequence, and

13 wherein, if the near-optimal code sequence is not found in a present invocation, for a next  
14 revocation of the automatic theorem prover if the proof succeeds the cycle budget K is doubled  
15 ( $K:=K*2$ ) and if the proof fails the cycle budget is bisected ( $K:=K/2$ ) and a new K-cycled  
16 program computing the program fragment that is embedded in the failed proof is extracted.

1 10. (Original) The method of claim 9, wherein the program fragment is presented to the  
2 automatic theorem prover as a set of guarded multi-assignments each including a guard and a  
3 multi-assignment that can be performed only when its respective guard is true.

1 11. (Previously Presented) The method of claim 10, wherein the set of guarded multi-  
2 assignments is compiled by instantiating universal facts about operators including machine and  
3 non-machine terms, wherein each instance of operators provides a way for computing a  
4 corresponding multi-assignment.

1 12. (Original) The method of claim 11, wherein the ways for computing the multi-  
2 assignments are encoded in a graph.

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- 1 13. (Original) The method of claim 12, wherein the graph is an equivalence graph (e-graph)  
2 formed as a directed acyclic graph.
- 1 14. (Previously Presented) The method of claim 12, wherein the graph is transformed in the  
2 presence of equalities between nodes.
- 1 15. (Previously Presented) The method of claim 12, wherein the graph is submitted for the  
2 extraction of the near optimal code sequence, the extraction using a description of the target  
3 computer architecture for formulating a boolean satisfiability problem a solution of which is  
4 found for the minimum cycle budget K via a satisfiability search.
- 1 16. (Original) The method of claim 12, wherein for a multi-assignment of the size n, an e-  
2 graph with a size order of n represents  $2^n$  distinct ways of computing the multi-assignment.
- 1 17. (Original) The method of claim 9, wherein the extraction of the near optimal code  
2 sequence is done from a formulation of a boolean satisfiability problem using a set of boolean  
3 unknowns that are one-to-one corresponding to a solution of the boolean satisfiability problem,  
4 the solution corresponding to a budget-cycle machine program where the budget is the minimum  
5 cycle budget K.
- 1 18. – 19. (Cancelled)
- 1 20. (Original) The method of claim 1 wherein the automatic theorem prover performs  
2 refutation-based automatic theorem proving.
- 1 21. (Original) The method of claim 9 wherein the automatic theorem prover performs  
2 refutation-based automatic theorem proving.

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1 22. (Previously Presented) A method for automatic generation of a near-optimal code  
2 sequence for execution on a computer, comprising:  
3 applying automatic theorem-proving to a code sequence generator, including  
4 introducing a multi-assignment to the code sequence generator,  
5 producing, by the code sequence generator based on the multi-assignment, a  
6 number of possible plans for creating the near-optimal code sequence, and  
7 performing, by the code sequence generator, planning with a satisfiability search  
8 to select an optimal plan from among the possible plans for automatically producing the near-  
9 optimal code sequence, wherein performing the planning with the satisfiability search is repeated  
10 a plurality of times for plural machine cycle budgets to find the optimal plan associated with a  
11 predetermined machine cycle budget.

1 23. (Original) A method as in claim 22, wherein the multi-assignment includes goal terms  
2 that specify what result the near-optimal code sequence is expected to produce, and wherein the  
3 applying automatic theorem proving further includes initializing a term graph with the goal terms  
4 whereby nodes of the term graph receive the goal terms.

1 24. (Previously Presented) A method as in claim 23, further comprising:  
2 introducing instances of universal facts that are relevant to the near-optimal code  
3 sequence, and  
4 augmenting the term graph with equivalence relations between the goal terms and  
5 corresponding instances of the universal facts by matching the universal facts against the term  
6 graph.

1 25. (Previously Presented) A method as in claim 23, wherein values of the goal terms are  
2 computed into registers of the computer, the registers being specified in the multi-assignment.

1 26. (Original) A method as in claim 24, wherein the term graph is augmented by the  
2 equivalence relations on its nodes to produce an equivalence graph (e-graph).

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- 1 27. (Previously Presented) A method as in claim 26, further comprising transforming the  
2 e-graph into a transformed e-graph that is provided to the planning with the satisfiability search.
- 1 28. (Original) A method as in claim 24, wherein the satisfiability search produces the near-  
2 optimal code sequence for achieving values corresponding to the goal terms.
- 1 29. (Previously Presented) A method as in claim 23, wherein the near-optimal code sequence  
2 is created from the term graph by iteratively solving a satisfiability problem with the machine  
3 cycle budgets until an optimal code sequence is found.
- 1 30. (Original) A method as in claim 24, wherein the universal facts are available in a file and  
2 are introduced as an input to the code sequence generator so that the universal facts can be  
3 changed without changing the code sequence generator.
- 1 31. (Original) A method as in claim 24, wherein the universal facts express properties of  
2 operators in the goal terms.
- 1 32. (Original) A method as in claim 25, wherein the term graph is initialized with node terms  
2 representing the goal terms.
- 1 33. (Cancelled)
- 1 34. (Previously Presented) A method as in claim 22, wherein the predetermined machine  
2 cycle budget is a minimal machine cycle budget.
- 1 35. (Original) A method as in claim 22, wherein the satisfiability search is a goal-directed  
2 search.

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1 36. (Currently Amended) A code sequence generation tool for automatic generation of a  
2 near-optimal code sequence executable on a computer, comprising:  
3 an input capable of receiving a multi-assignment;  
4 a matcher responsive to the multi-assignment and producing, via matching of the  
5 multi-assignment and facts regarding operators computable in [[a]] the computer, a number of  
6 possible plans for creating the near-optimal code sequence; and  
7 a planner configured to select via a satisfiability search an optimal plan from among the  
8 possible plans produced by the matcher, the optimal plan corresponding to the near-optimal code  
9 sequence,  
10 wherein the code sequence generation tool is configured to invoke the matcher and the  
11 planner thereby implementing automatic theorem-proving for automatically generating the near-  
12 optimal code sequence.

1 37. (Original) A code sequence generation tool as in claim 36 being further configured for  
2 producing the optimal code sequence using a goal-oriented, cycle budget limited code sequence  
3 in generating the near-optimal code sequence.

1 38. (Original) A code sequence generation tool as in claim 36 wherein the planner includes a  
2 constraint generator and a solver, the code sequence generation tool further comprising an input  
3 configured for introducing architectural constraints to the constraint generator which the  
4 constraint generator uses in creating a set of boolean unknowns for the solver.

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1 39. (Currently Amended) A code sequence generation tool for automatic generation of a  
2 near-optimal code sequence executable on a computer, comprising:  
3 an input capable of receiving a multi-assignment;  
4 matching means responsive to the multi-assignment and producing, via matching of the  
5 multi-assignment and facts regarding operators computable in [[a]] the computer, a number of  
6 possible plans for creating the near-optimal code sequence; and  
7 planning means configured to select via a satisfiability search an optimal plan from  
8 among the possible plans produced by the matching means, the optimal plan corresponding to  
9 the near-optimal code sequence,  
10 wherein the code sequence generation tool is configured to invoke the matching means  
11 and the planning means thereby implementing automatic theorem-proving for automatically  
12 generating the near-optimal code sequence.

1 40. (Cancelled)

1 41. (Previously Presented) The method of claim 22, further comprising executing the code  
2 sequence generator as a computer-executed code sequence generator.

1 42. (Previously Presented) The code sequence generation tool of claim 36, wherein the  
2 planner is invocable a plurality of times for plural machine cycle budgets, the planner to select  
3 the optimal plan associated with a minimum machine cycle budget from among the plural  
4 machine cycle budgets.

1 43. (Previously Presented) The code sequence generation tool of claim 39, wherein the  
2 planning means is invocable a plurality of times for plural machine cycle budgets, the planner to  
3 select the optimal plan associated with a minimum machine cycle budget from among the  
4 machine cycle budgets.



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1 44. (Currently Amended) A method of producing a near-optimal code sequence for at least a  
2 fragment of a program executable on a computer, comprising:  
3 inputting expressions corresponding to the fragment of the program to a  
4 computer-executable code sequence generator;  
5 generating, by the code sequence generator based on the input expressions and facts  
6 regarding operators computable in [[a]] the computer, a data structure representing plural ways  
7 of computing the expressions; and  
8 performing a satisfiability search by the code sequence generator to select one of the  
9 ways as an optimal solution associated with a minimum machine cycle budget, the optimal  
10 solution corresponding to the near-optimal code sequence.

1 45. (Previously Presented) The method of claim 44, wherein performing the satisfiability  
2 search is repeated plural times for plural machine cycle budgets.

1 46. (Previously Presented) A computer-readable medium embodying computer program  
2 code configured to cause a computer to generate a near-optimal code sequence for at least a  
3 fragment of a program, comprising:  
4 inputting expressions corresponding to the fragment of the program to a code sequence  
5 generator;  
6 generating, by the code sequence generator based on the input expressions and facts  
7 regarding operators computable in a computer, a data structure representing plural ways of  
8 computing the expressions; and  
9 performing a satisfiability search by the code sequence generator to select one of the  
10 ways as an optimal solution associated with a minimum machine cycle budget, the optimal  
11 solution corresponding to the near-optimal code sequence.

1 47. (Previously Presented) The computer-readable medium of claim 46, wherein performing  
2 the satisfiability search is repeated plural times for plural machine cycle budgets.